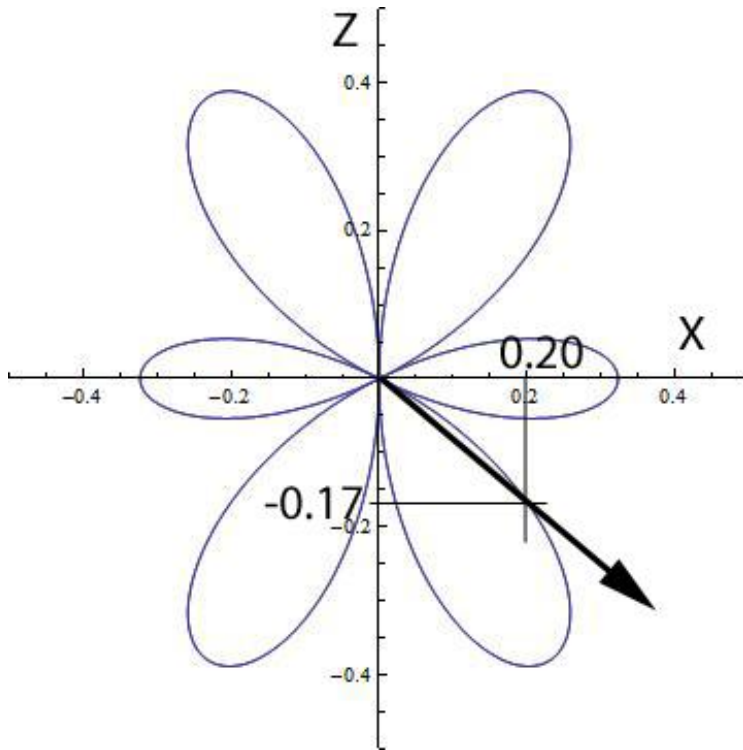


Reading: Griffiths, pages 131-160

- 1) The graph below shows the representation of  $Y_l^m(\theta, \phi)$ , the spherical harmonic for  $l = 3, m = 1$ .



What is the magnitude and phase of  $Y_3^1(\theta, \phi)$  for the angle  $\theta = 130^\circ, \phi = 0^\circ$  (indicated by the arrow in the graph)?

- a)  $|Y_3^1| = 0.26$  and phase = 0
- b)  $|Y_3^1| = 0.26$  and there is not enough info to determine phase
- c)  $|Y_3^1| = 0.2$  and phase =  $130^\circ$
- d)  $|Y_3^1| = 0.17$  and phase =  $130^\circ$
- e)  $|Y_3^1| = -0.26$  and phase = 0

TURN OVER

2) The normalized hydrogen wave functions are given by:

$$\psi_{nlm} = \sqrt{\left(\frac{2}{na}\right)^3 \frac{(n-l-1)!}{2n[(n+l)!]^3}} e^{-\frac{r}{na}} \left(\frac{2r}{na}\right)^l \left[ L_{n-l-1}^{2l+1}\left(\frac{2r}{na}\right) \right] Y_l^m(\theta, \phi)$$

What is the radial wavefunction  $R_{20}$  ( $n = 2, l = 0$ )? You may use the table below:

**TABLE 4.6:** Some associated Laguerre polynomials,  $L_{q-p}^p(x)$ .

$L_0^0 = 1$	$L_0^2 = 2$
$L_1^0 = -x + 1$	$L_1^2 = -6x + 18$
$L_2^0 = x^2 - 4x + 2$	$L_2^2 = 12x^2 - 96x + 144$
$L_0^1 = 1$	$L_0^3 = 6$
$L_1^1 = -2x + 4$	$L_1^3 = -24x + 96$
$L_2^1 = 3x^2 - 18x + 18$	$L_2^3 = 60x^2 - 600x + 1200$

- $\frac{1}{\sqrt{2}} a^{-3/2} \left(1 - \frac{r}{2a}\right) \exp\left(-r/2a\right)$
- $\frac{1}{\sqrt{2}} a^{-3/2} \left(1 + \frac{r}{2a}\right) \exp\left(-r/2a\right)$
- $\frac{1}{\sqrt{2}} a^{-3/2} \left(4 - \frac{r}{a}\right) \exp\left(-r/2a\right)$
- $\frac{1}{\sqrt{2}} a^{-3/2} \left(1 - 4\frac{r}{a}\right) \exp\left(-r/2a\right)$
- $\frac{1}{\sqrt{2}} a^{-3/2} \left(1 + 4\frac{r}{a}\right) \exp\left(-r/2a\right)$